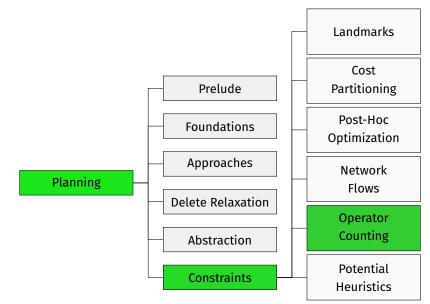
Automated Planning F10. Operator Counting

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based on slides from the AI group at the University of Basel

Content of this Course



Introduction

Reminder: Flow Heuristic

In the previous chapter, we used flow constraints to describe how often operators must be used in each plan.

Example (Flow Constraints)

Let Π be a planning problem with operators $\{o_{red}, o_{green}, o_{blue}\}$. The flow

constraint for some atom a is the constraint

$$1 + Count_{o_{green}} = Count_{o_{red}}$$
 if

- a is true in the initial state o_{green} produces a
- *a* is false in the goal

Ored consumes a

In natural language, the flow constraint expresses that

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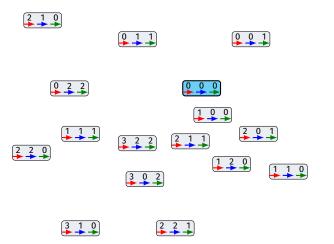
- a is true in the initial state o_{green} produces a
- *a* is false in the goal

- Ored consumes a
- In natural language, the flow constraint expresses that

every plan uses ored once more than ogreen.

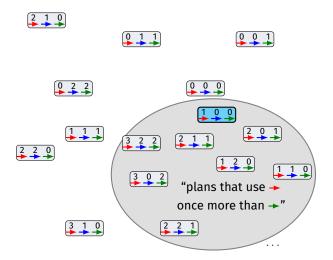
Reminder: Flow Heuristic

Let us now observe how each flow constraint alters the operator count solution space.



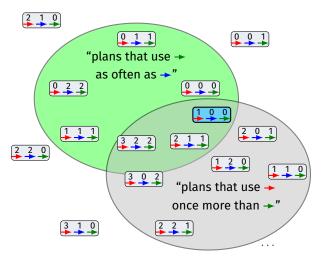
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Reminder: Flow Heuristic

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Operator-counting Framework

Operator Counting

Operator counting

- generalizes this idea to a framework that allows to admissibly combine different heuristics.
- uses linear constraints . . .
- ... that describe number of occurrences of an operator ...
- ... and must be satisfied by every plan.
- provides declarative way to describe knowledge about solutions.
- allows reasoning about solutions to derive heuristic estimates.

Operator-counting Constraint

Definition (Operator-counting Constraints)

Let Π be a planning task with operators O and let s be a state. Let \mathcal{V} be the set of integer variables $Count_o$ for each $o \in O$.

A linear inequality over \mathcal{V} is called an operator-counting constraint for s if for every plan π for s setting each Count_o to the number of occurrences of o in π is a feasible variable assignment.

Operator-counting Heuristics

Definition (Operator-counting IP/LP Heuristic)

The operator-counting integer program IP_C for a set C of operator-counting constraints for state s is

 $\begin{array}{ll} \text{Minimize} & \sum_{o \in O} cost(o) \cdot \text{Count}_o & \text{subject to} \\ \text{C and Count}_o \geq 0 \text{ for all } o \in O, \end{array}$

where O is the set of operators.

The IP heuristic h_C^{IP} is the objective value of IP_C, the LP heuristic h_C^{LP} is the objective value of its LP-relaxation. If the IP/LP is infeasible, the heuristic estimate is ∞ .

Operator-counting Constraints

- Adding more constraints can only remove feasible solutions.
- Fewer feasible solutions can only increase the objective value.
- Higher objective value means better informed heuristic
- \Rightarrow Have we already seen other operator-counting constraints?

Reminder: Minimum Hitting Set for Landmarks

Variables

Non-negative variable Applied_o for each operator o

Objective

Minimize $\sum_{o} cost(o) \cdot Applied_{o}$

$$\sum_{o \in L} \mathsf{Applied}_o \geq 1 \text{ for all landmarks } L$$

Operator Counting with Disjunctive Action Landmarks

Variables

Non-negative variable Counto for each operator o

Objective

Minimize $\sum_{o} cost(o) \cdot Count_{o}$

$$\sum_{o \in L} Count_o \ge 1 \text{ for all landmarks } L$$

Reminder: Post-hoc Optimization Heuristic

For set of abstractions $\{\alpha_1, \ldots, \alpha_n\}$:

Variables

Non-negative variables X_o for all operators $o \in O$

 X_o is cost incurred by operator o

Objecti<u>ve</u>

Minimize $\sum_{o \in O} X_o$

$$\sum_{o \in O:o \text{ relev. for } \alpha} X_o \ge h^{\alpha}(s) \quad \text{for } \alpha \in \{\alpha_1, \dots, \alpha_n\}$$
$$X_o \ge 0 \qquad \text{for all } o \in O$$

Operator Counting with Post-hoc Optimization Constraints

For set of abstractions $\{\alpha_1, \ldots, \alpha_n\}$:

Variables

Non-negative variables $Count_o$ for all operators $o \in O$

 $Count_o \cdot cost(o)$ is cost incurred by operator o

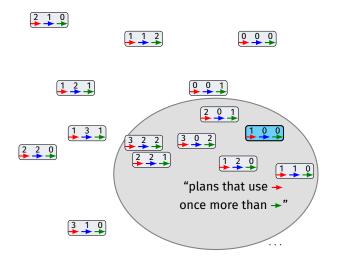
Objective

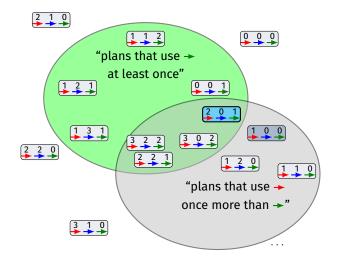
Minimize $\sum_{o \in O} cost(o) \cdot Count_o$

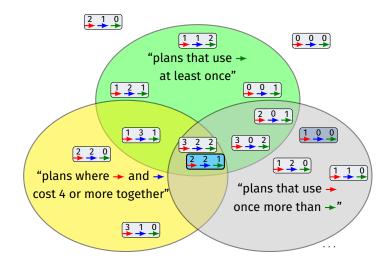
$$\sum_{o \in O:o \text{ relev. for } \alpha} \operatorname{cost}(o) \cdot \operatorname{Count}_{o} \ge h^{\alpha}(s) \quad \text{for } \alpha \in \{\alpha_{1}, \dots, \alpha_{n}\}$$
$$\operatorname{cost}(o) \cdot \operatorname{Count}_{o} \ge 0 \qquad \text{for all } o \in O$$

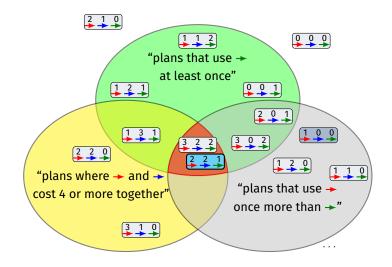
Operator-counting Framework

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Further Examples?

- The definition of operator-counting constraints can be extended to groups of constraints and auxiliary variables.
- With this extended definition we could also cover more heuristics, e.g., the perfect relaxation heuristic h⁺.

Properties

Theorem (Operator-counting Heuristics are Admissible)

The IP and the LP heuristic are admissible.

Theorem (Dominance)

Let C and C' be sets of operator-counting constraints for s and let $C \subseteq C'$. Then $IP_C \leq IP_{C'}$ and $LP_C \leq LP_{C'}$.

Adding more constraints can only improve the heuristic estimate.

Heuristic Combination

Operator counting as heuristic combination

- Multiple operator-counting heuristics can be combined by computing h^{LP}_C/h^P_C for the union of their constraints.
- This is an admissible combination.
 - Never worse than maximum of individual heuristics
 - Sometimes even better than their sum
- We already know a way of admissibly combining heuristics: cost partitioning.
 - \Rightarrow How are they related?

Operator-counting Framework

Properties

Connection to Cost Partitioning

Theorem

Let C_1, \ldots, C_n be sets of operator-counting constraints for s and $C = \bigcup_{i=1}^{n} C_i$. Then h_C^{LP} is the optimal general cost partitioning over the heuristics $h_{C_i}^{LP}$.

Comparison to Optimal Cost Partitioning

- some heuristics are more compact if expressed as operator counting
- some heuristics cannot be expressed as operator counting
- operator counting IP even better than optimal cost partitioning
- Cost partitioning maximizes, so heuristics must be encoded perfectly to guarantee admissibility.
 Operator counting minimizes, so missing information just makes the

heuristic weaker.

Summary

Summary

- Many heuristics can be formulated in terms of operator-counting constraints.
- The operator counting heuristic framework allows to combine the constraints and to reason on the entire encoded declarative knowledge.
- The heuristic estimate for the combined constraints can be better than the one of the best ingredient heuristic but never worse.
- Operator counting is equivalent to optimal general cost partitioning over individual constraints.