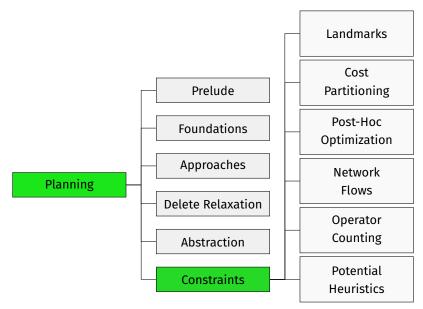
# **Automated Planning**

F1. Constraints: Introduction

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#### Content of this Course



# **Constraint-based Heuristics**

# Coming Up with Heuristics in a Principled Way

#### General Procedure for Obtaining a Heuristic

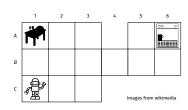
Solve a simplified version of the problem.

#### Major ideas for heuristics in the planning literature:

- delete relaxation
- abstraction
- critical paths
- landmarks
- network flows
- potential heuristic

Landmarks, network flows and potential heuristics are based on constraints that can be specified for a planning task.

### Constraints: Example



FDR planning task  $\langle V, I, O, \gamma \rangle$  with

- $\blacksquare$   $V = \{robot-at, dishes-at\}$  with
  - $\bullet$  dom(robot-at) = {A1, ..., C3, B4, A5, ..., B6}
  - dom(dishes-at) = {Table, Robot, Dishwasher}
- $I = \{ robot at \mapsto C1, dishes at \mapsto Table \}$
- operators
  - move-x-y to move from cell x to adjacent cell y
  - pickup dishes, and
  - load dishes into the dishwasher.
- $\mathbf{v} = (robot-at = B6) \land (dishes-at = Dishwasher)$

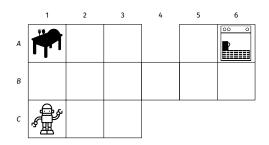
#### Constraints

Some heuristics exploit constraints that describe something that holds in every solution of the task.

For instance, every solution is such that

a variable takes a certain value in at least one visited state.
 (a fact landmark constraint)

#### Which values do robot-at and dishes-at take in every solution?

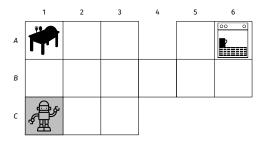








#### Which values do robot-at and dishes-at take in every solution?



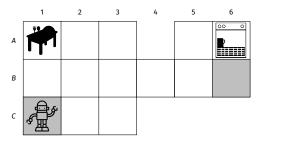






robot-at = C1, dishes-at = Table (initial state)

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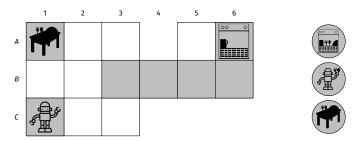






- robot-at = C1, dishes-at = Table (initial state)
- robot-at = B6, dishes-at = Dishwasher (goal state)

#### Which values do robot-at and dishes-at take in every solution?



- robot-at = C1, dishes-at = Table (initial state)
- robot-at = B6, dishes-at = Dishwasher (goal state)
- robot-at = A1, robot-at = B3, robot-at = B4, robot-at = B5, robot-at = A6, dishes-at = Robot

#### Constraints

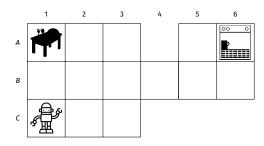
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For instance, every solution is such that

- a variable takes some value in at least one visited state.
   (a fact landmark constraint)
- an action must be applied.(an action landmark constraint)

# Action Landmarks: Example

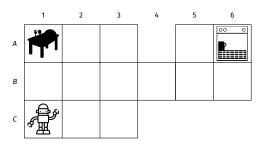
#### Which actions must be applied in every solution?

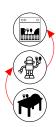




# Action Landmarks: Example

#### Which actions must be applied in every solution?

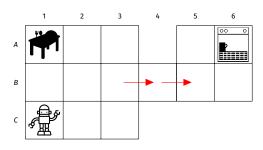


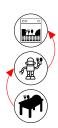


- pickup
- load

# Action Landmarks: Example

#### Which actions must be applied in every solution?





- pickup
- load
- move-B3-B4
- move-B4-B5

#### Constraints

Some heuristics exploit constraints that describe something that holds in every solution of the task.

For instance, every solution is such that

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#### Constraints

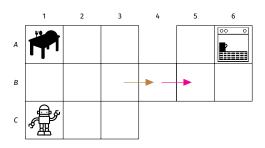
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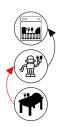
For instance, every solution is such that

- a variable takes some value in at least one visited state.
   (a fact landmark constraint)
- at least one action from a set of actions must be applied.
   (a disjunctive action landmark constraint)

# Disjunctive Action Landmarks: Example

#### Which set of actions is such that at least one must be applied?

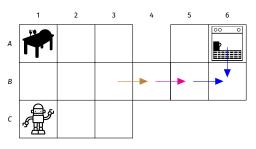


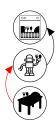


- {pickup}
- {load}
- {move-B3-B4}
- {move-B4-B5}

### Disjunctive Action Landmarks: Example

#### Which set of actions is such that at least one must be applied?





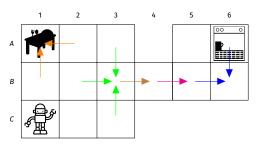
■ {pickup}

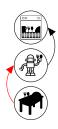
■ {move-A6-B6, move-B5-B6}

- {load}
- {move-B3-B4}
- {move-B4-B5}

### Disjunctive Action Landmarks: Example

#### Which set of actions is such that at least one must be applied?





- {pickup}
- {load}
- {move-B3-B4}
- {move-B4-B5}

- {move-A6-B6, move-B5-B6}
- {move-A3-B3, move-B2-B3, move-C3-B3}
- {move-B1-A1, move-A2-A1}
- ..

#### **Constraints**

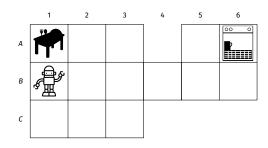
Some heuristics exploit constraints that describe something that holds in every solution of the task.

For instance, every solution is such that

- a variable takes some value in at least one visited state.
   (a fact landmark constraint)
- at least one action from a set of actions must be applied.
   (a disjunctive action landmark constraint)
- fact consumption and production is "balanced".
   (a network flow constraint)

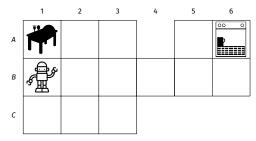
### Network Flow: Example

Consider the fact robot-at = B2. How often are actions used that enter this cell?



### Network Flow: Example

Consider the fact robot-at = B2. How often are actions used that enter this cell?



Answer: as often as actions that leave this cell

If Count<sub>o</sub> denotes how often operator o is applied, we have:

$$\begin{aligned} & \text{Count}_{\text{move-A1-B1}} + \text{Count}_{\text{move-B2-B1}} + \text{Count}_{\text{move-C1-B1}} = \\ & \text{Count}_{\text{move-B1-A1}} + \text{Count}_{\text{move-B1-B2}} + \text{Count}_{\text{move-B1-C1}} \end{aligned}$$

# **Multiple Heuristics**

### **Combining Admissible Heuristics Admissibly**

#### Major ideas to combine heuristics admissibly:

- maximize
- canoncial heuristic (for abstractions)
- minimum hitting set (for landmarks)
- cost partitioning
- operator counting

Often computed as solution to a (integer) linear program.

# Combining Heuristics Admissibly: Example

#### Example

Consider an FDR planning task  $\langle V, I, \{o_1, o_2, o_3, o_4\}, \gamma \rangle$  with  $V = \{v_1, v_2, v_3\}$  with  $dom(v_1) = \{A, B\}$  and  $dom(v_2) = dom(v_3) = \{A, B, C\}, I = \{v_1 \mapsto A, v_2 \mapsto A, v_3 \mapsto A\},$   $o_1 = \langle v_1 = A, v_1 := B, 1 \rangle$   $o_2 = \langle v_2 = A \wedge v_3 = A, v_2 := B \wedge v_3 := B, 1 \rangle$   $o_3 = \langle v_2 = B, v_2 := C, 1 \rangle$   $o_4 = \langle v_3 = B, v_3 := C, 1 \rangle$ 

and 
$$\gamma = (v_1 = B) \land (v_2 = C) \land (v_3 = C)$$
.

Consider all atomic projections. By using additivity for orthogonal abstractions, which heuristic estimates can we sum up admissibly?

### Combining Heuristics Admissibly: Example

#### Example

Consider an FDR planning task  $\langle V, I, \{o_1, o_2, o_3, o_4\}, \gamma \rangle$  with  $V = \{v_1, v_2, v_3\}$  with  $dom(v_1) = \{A, B\}$  and  $dom(v_2) = dom(v_3) = \{A, B, C\}, I = \{v_1 \mapsto A, v_2 \mapsto A, v_3 \mapsto A\}$ ,

$$o_1 = \langle v_1 = A, v_1 := B, 1 \rangle$$
  
 $o_2 = \langle v_2 = A \wedge v_3 = A, v_2 := B \wedge v_3 := B, 1 \rangle$   
 $o_3 = \langle v_2 = B, v_2 := C, 1 \rangle$   
 $o_4 = \langle v_3 = B, v_3 := C, 1 \rangle$ 

and 
$$\gamma = (v_1 = B) \land (v_2 = C) \land (v_3 = C)$$
.

Consider all atomic projections. By using additivity for orthogonal abstractions, which heuristic estimates can we sum up admissibly?

Answer: Let  $h_i := h^{v_i}$ . Then  $h = \max\{h_1 + h_2, h_1 + h_3\}$  is admissible.

### Reminder: Orthogonality and Additivity

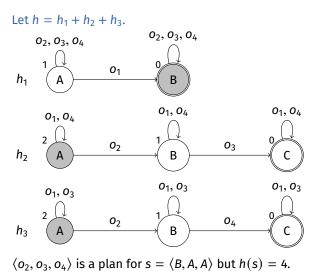
Why can we add  $h_1$  and  $h_2$  ( $h_1$  and  $h_3$ ) admissibly?

#### Theorem (Additivity for Orthogonal Abstractions)

Let  $h^{\alpha_1}, \ldots, h^{\alpha_n}$  be abstraction heuristics of the same transition system such that  $\alpha_i$  and  $\alpha_i$  are orthogonal for all  $i \neq j$ .

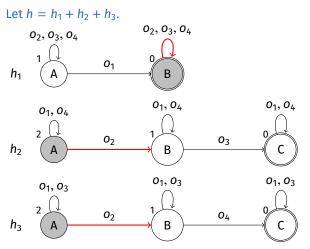
Then  $\sum_{i=1}^n h^{\alpha_i}$  is a safe, goal-aware, admissible and consistent heuristic for  $\Pi$ .

# Combining Heuristics (In)admissibly: Example



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# Combining Heuristics (In)admissibly: Example



 $\langle o_2, o_3, o_4 \rangle$  is a plan for  $s = \langle B, A, A \rangle$  but h(s) = 4. Heuristics  $h_2$  and  $h_3$  both account for the single application of  $o_2$ .

## **Prevent Inadmissibility**

The reason that  $h_2$  and  $h_3$  are not additive is because the cost of  $o_2$  is considered in both.

Is there anything we can do about this?

## **Prevent Inadmissibility**

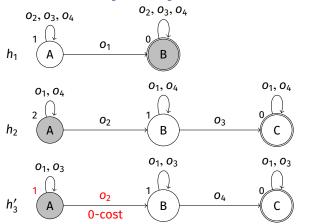
The reason that  $h_2$  and  $h_3$  are not additive is because the cost of  $o_2$  is considered in both.

Is there anything we can do about this?

Solution: We can ignore the cost of  $o_2$  in one heuristic by setting its cost to 0 (e.g.,  $cost_3(o_2) = 0$ ).

### Combining Heuristics Admissibly: Example

Let  $h' = h_1 + h_2 + h'_3$ , where  $h'_3 = h^{v_3}$  assuming  $cost_3(o_2) = 0$ .



 $\langle o_2, o_3, o_4 \rangle$  is an optimal plan for  $s = \langle B, A, A \rangle$  and h'(s) = 3 an admissible estimate.

# **Cost partitioning**

Using the cost of every operator only in one heuristic is called a zero-one cost partitioning.

### Cost partitioning

Using the cost of every operator only in one heuristic is called a zero-one cost partitioning.

More generally, heuristics are additive if all operator costs are distributed in a way that the sum of the individual costs is no larger than the cost of the operator.

This can also be expressed as a constraint, the cost partitioning constraint:

$$\sum_{i=1}^{n} cost_{i}(o) \le cost(o) \text{ for all } o \in O$$

(more details later)

# **Summary**

### Summary

- Landmarks and network flows are constraints that describe something that holds in every solution of the task.
- Heuristics can be combined admissibly if the cost partitioning constraint is satisfied.