

# New Refinement Strategies for Cartesian Abstractions



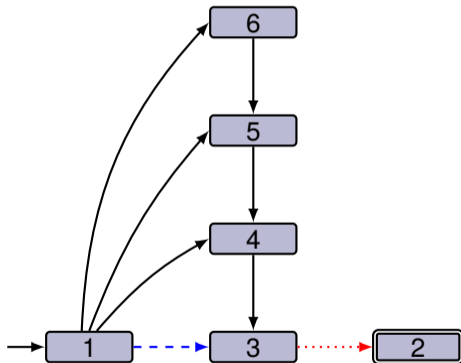
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<sup>1</sup>University of Freiburg, Germany

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# Motivation



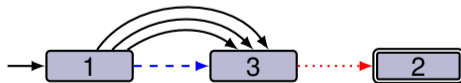
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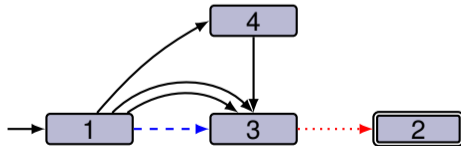
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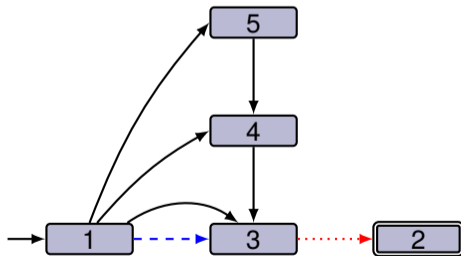
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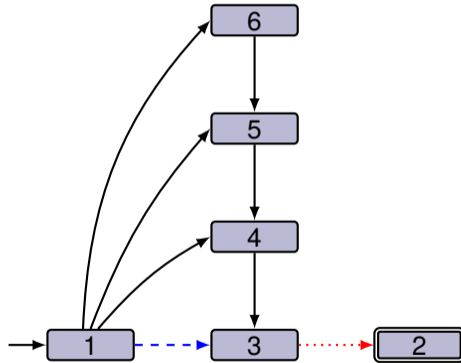


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# New refinement strategies

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## Counterexample-Guided Cartesian Abstraction Refinement (CEGAR)

- Repeatedly find counterexamples
  - I.e., abstract plans that **fail** for the concrete task
  - Repair the flaw by **splitting** a state



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## Contribution

- Consider **all** optimal abstract plans
- New refinement strategies = **flaw** + **split** selection strategies

# How can we find all flaws?

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## Flaw Search

- Consider **all** optimal abstract plans
- Depth-first search in the concrete transition system
- Consider only  **$f$ -optimal transitions** of the abstraction
- **Collect** all encountered **flaws**
- Goal state expanded  $\rightsquigarrow$  optimal **concrete** plan
- Open list empty  $\rightsquigarrow$  **all flaws** found

# Flaw selection strategy

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## FIRST strategy [SH18]

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- Selects the **first** flaw found for  $\pi$
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## BATCH strategy

- Search for all flaws
- Return a concrete plan if the flaw search found one
- **Iteratively** repairs the flaw with the **lowest  $h$ -value**
- Attention: repairing a flaw can **change** the abstraction!
- Check if  $h$ -values of flaws have changed
- Repair **all** flaws that maintain the  $h$ -value

## Flaw selection strategy – Theoretical results

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FIRST/MAXH can lead to **arbitrarily larger** abstractions until a concrete solution is found, compared to MINH/BATCH.

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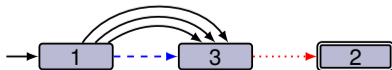
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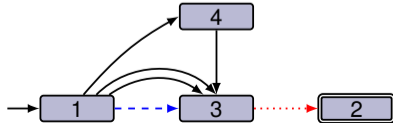
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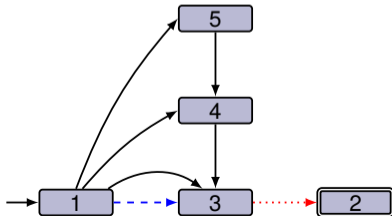
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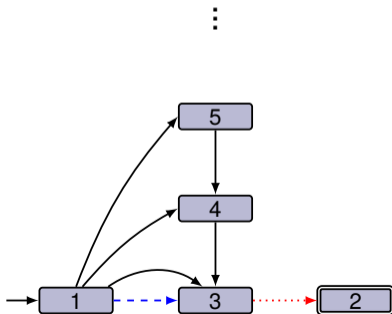
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# Split selection strategy

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- I.e., how to split the abstract state



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## MAXREFINED strategy [SH18]

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## COVER strategy

- Consider **multiple** flaws at once
- Chooses split that addresses the **most** flaws at once

# Experiments

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- Implemented **refinement strategies** in SCORPION [Sei18]
- Planning tasks from **optimal track** of IPCs
- 15 min and 3.5GB for CEGAR
- 30 min and 4GB memory for  $A^* + h^{\text{CEGAR}}$

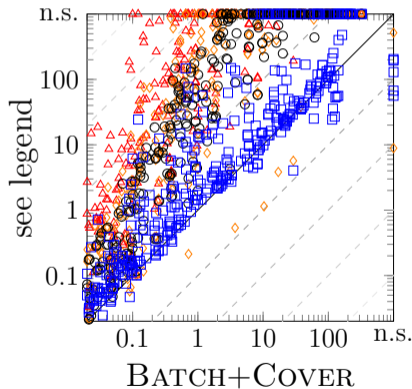
# Experiments – Coverage

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Strategy	MAXREFINED			COVER	
	FIRST	MAXH	MINH	MINH	BATCH
<b>CEGAR</b>	499	345	382	393	<b>534</b>

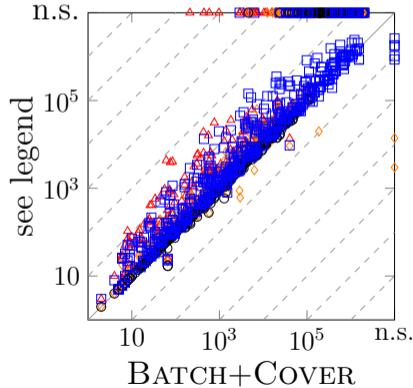
# Experiments – Runtime

□ FIRST+MAXREFINED    △ MAXH+MAXREFINED    ◇ MINH+MAXREFINED    ○ MINH+COVER



# Experiments – Abstraction Size

□ FIRST+MAXREFINED    △ MAXH+MAXREFINED    ◇ MINH+MAXREFINED    ○ MINH+COVER



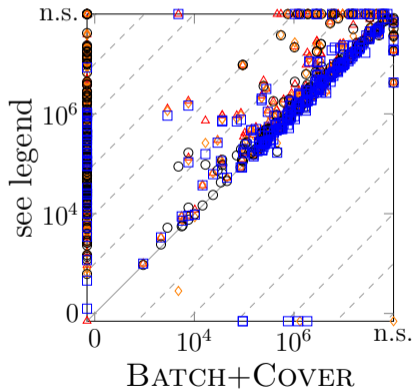
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Strategy	MAXREFINED			COVER	
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CEGAR	499	345	382	393	<b>534</b>
$A^* + h^{\text{CEGAR}}$	802	780	792	797	<b>812</b>

# Experiments – Expansions

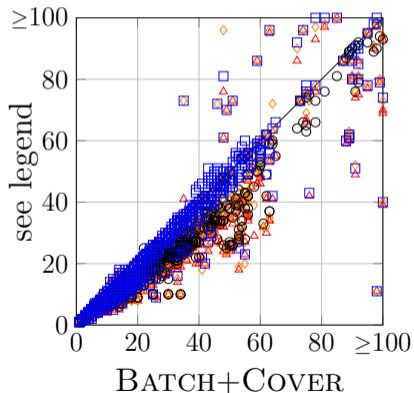
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# Experiments – Heuristic Accuracy

□ FIRST+MAXREFINED    △ MAXH+MAXREFINED    ◇ MINH+MAXREFINED    ○ MINH+COVER



# Conclusion

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- New refinement strategies for CEGAR  $\rightsquigarrow$  **flaw + split** selection strategies
- Flaw Search  $\rightsquigarrow$  determine **all** flaws simultaneously

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## Findings

- Refine states **close to the goal**
- Split states such that **multiple flaws** are repaired at once
- Repair as **many flaws** as possible in one step (batch)

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## Findings

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## Future work

- Compare refinement strategies for **multiple** Cartesian abstractions

# References I

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- [Sei18] Jendrik Seipp, *Fast Downward Scorpion*, IPC-9 Planner Abstracts, 2018, pp. 77–79.
- [SH18] Jendrik Seipp and Malte Helmert, *Counterexample-guided Cartesian abstraction refinement for classical planning*, JAIR **62** (2018), 535–577.