

# Decoupled Search for the Masses: A Novel Task Transformation for Classical Planning



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**Daniel Gnad**<sup>1</sup>

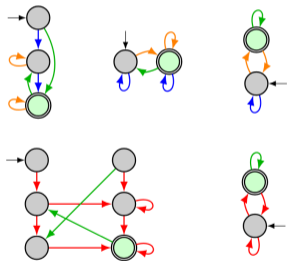
<sup>1</sup>Linköping University, Sweden

<sup>2</sup>University of Basel, Switzerland

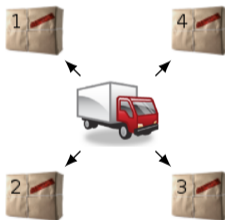
# Motivation

We often transform our planning task to make an efficient search possible!

Factored Transition System



Decoupled Search

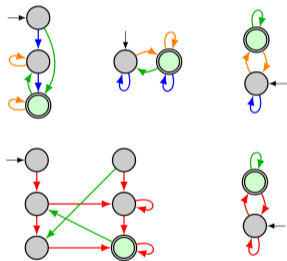


- ✓ Potentially exponentially more efficient
- ✓ Fully automated
- ✗ Alternative state representation  $\rightsquigarrow$  Specialized search algorithms

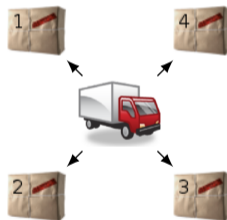
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## Satisficing Planning

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- Factoring  $\mathcal{F} = \langle C, \mathcal{L} \rangle$  of vars  $\mathcal{V}$ 
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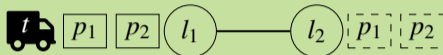
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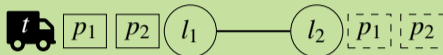


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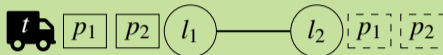


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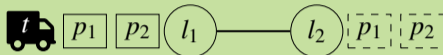
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$\mathcal{I}^{\mathcal{F}}: t = l_1$
$l_1 \quad l_2 \quad t$
<hr/>
$p_1 \quad 1 \quad 0 \quad 0$
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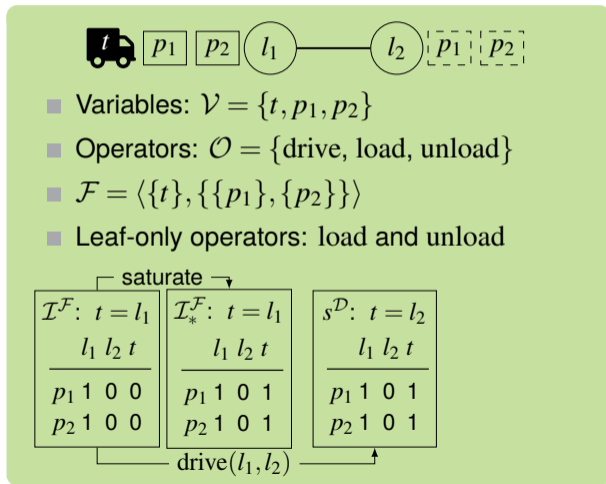
← saturate →

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$l_1 \ l_2 \ t$	$l_1 \ l_2 \ t$
$p_1 \ 1 \ 0 \ 0$	$p_1 \ 1 \ 0 \ 1$
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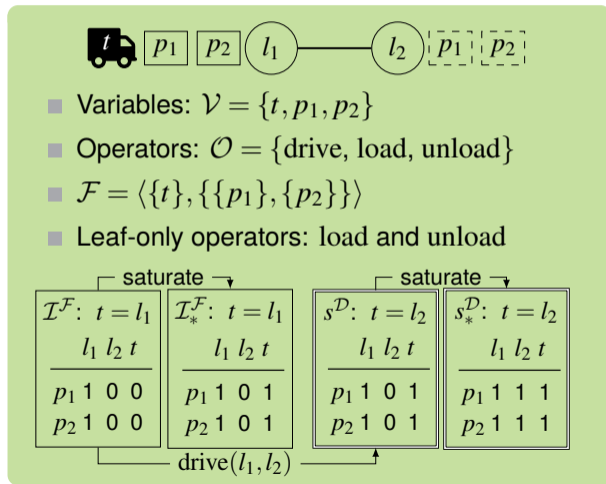
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Input: SAS<sup>+</sup> Planning Task  $\Pi = \langle \mathcal{V}, \mathcal{I}, \mathcal{G}, \mathcal{O} \rangle$

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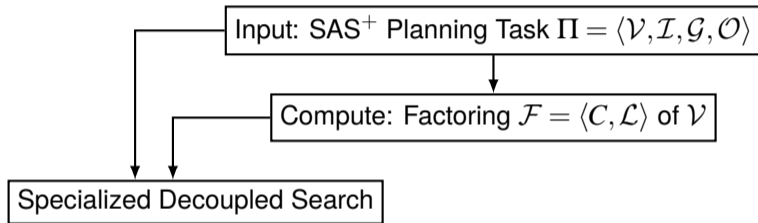


Compute: Factoring  $\mathcal{F} = \langle \mathcal{C}, \mathcal{L} \rangle$  of  $\mathcal{V}$

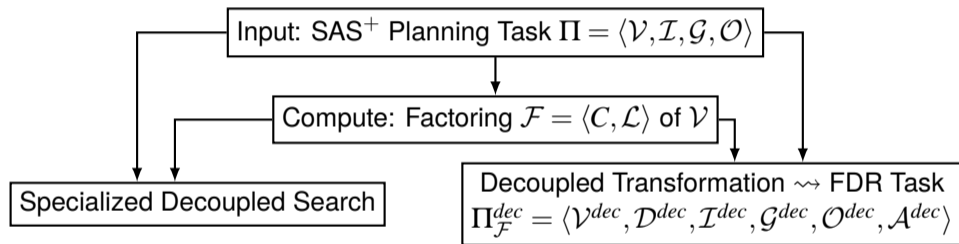


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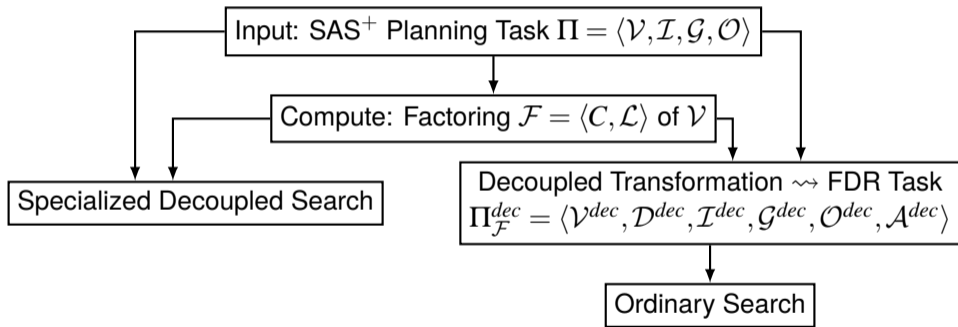
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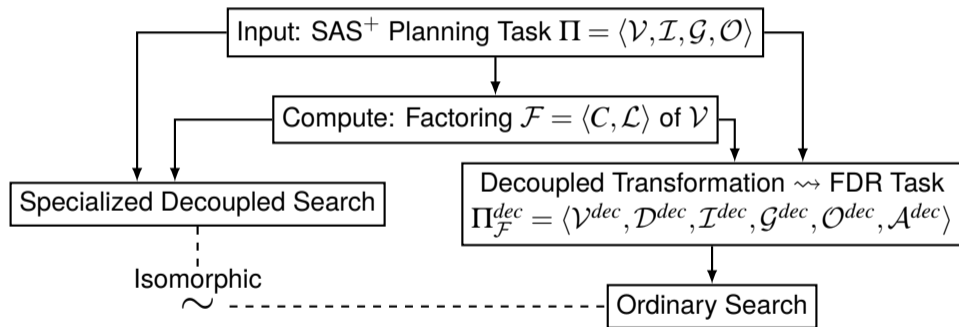
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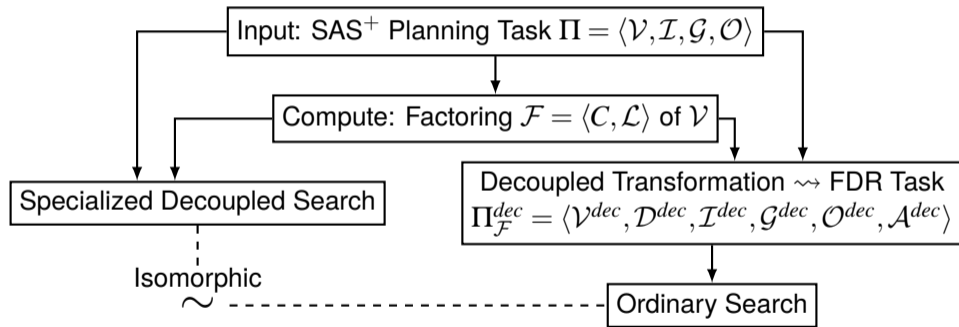
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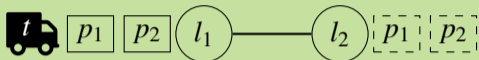
- Embodies decoupled search  $\rightsquigarrow$  Potential **exponentially smaller search space**
- No specialized algorithms  $\rightsquigarrow$  Past and future **planning techniques work out of the box**

# Decoupled Transformation

Leaf dynamics  $\rightsquigarrow$  Axioms!

Variables:

- $\mathcal{F} = \langle \{t\}, \{\{p_1\}, \{p_2\}\} \rangle$
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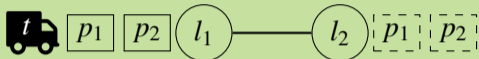


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$(p_1, t)$	0	$(p_1, t)$	
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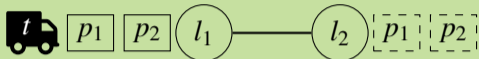
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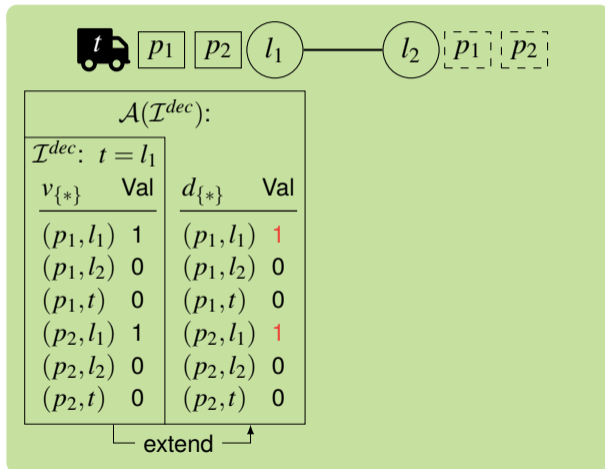
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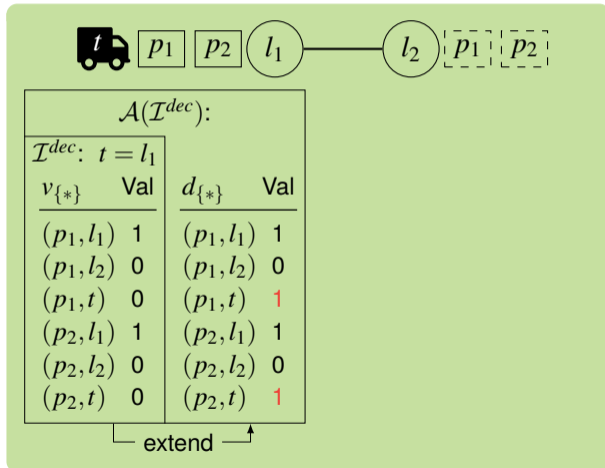
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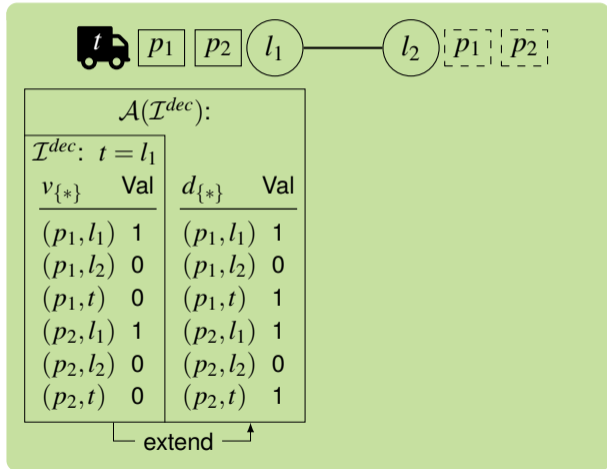
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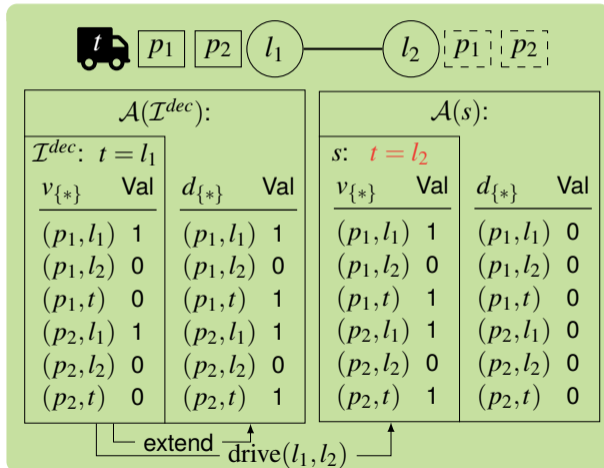
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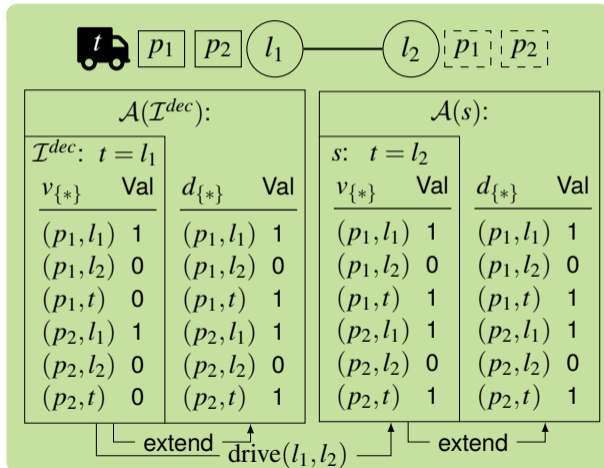
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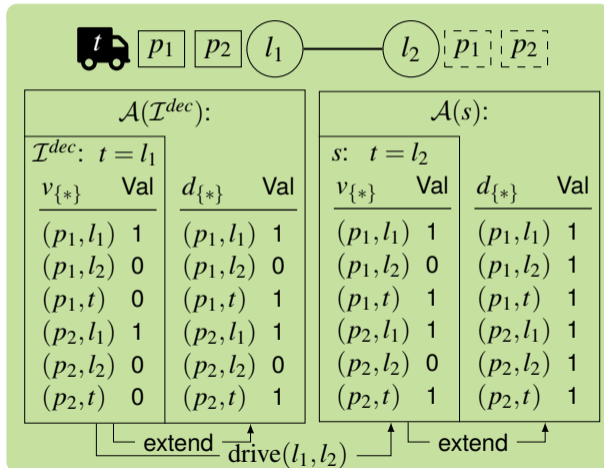
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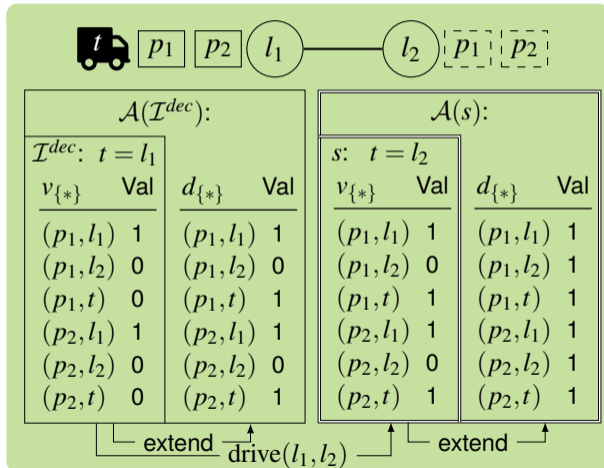
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# Isomorphic State Spaces

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- One-to-one mapping
  - ↷ Decoupled states  $\Leftrightarrow$  unextended states of  $\Pi_{\mathcal{F}}^{dec}$
- Similar relationship
  - ↷ Saturated decoupled states  $\Leftrightarrow$  extended states of  $\Pi_{\mathcal{F}}^{dec}$
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- Theorem: **Isomorphic** state spaces!

↪ Search algorithms applied on  $\Pi_{\mathcal{F}}^{dec}$  behave identically to specialized counterparts

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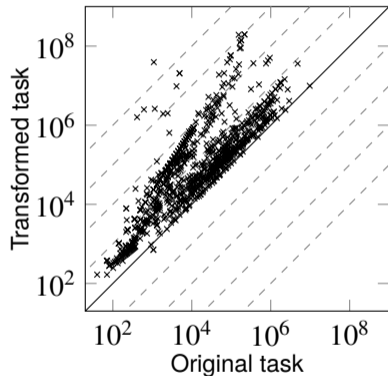
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## Related Work – Miura & Fukunaga (ICAPS 2017):

- Transforming a planning task into a more concise form using axioms
- $\rightsquigarrow$  A weaker form of a **single conclusive leaf**
- $\rightsquigarrow$  Special form of decoupled search
- $\rightsquigarrow$  We generalize it in multiple dimensions!

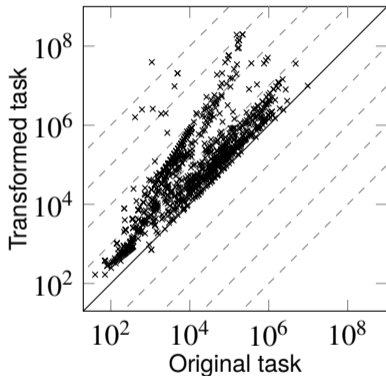
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Satisficing IPC Benchmark: 2106 tasks



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Time	<1s	<5s	<10s	<30s	<60s	≥60s	DNF
# Tasks	955	47	24	14	3	12	4

# Experiments – Planning Performance

Satisficing IPC Benchmark: 2106 tasks

Domain	GBFS( $h^{FF}$ , PO)			
	<i>dec</i>	<i>sas</i>	<i>gh</i>	<i>ts</i>
airport	12	<b>14</b>	11	13
data-net	9	10	5	<b>11</b>
floortile11	14	8	<b>17</b>	8
nomystery	16	9	<b>19</b>	10
tetris	9	<b>14</b>	11	2
transport14	<b>20</b>	9	<b>20</b>	<b>20</b>
...		...		
<b>Sum</b> 1059	944	912	<b>980</b>	915

*dec*: Decoupled Transformation  
*sas*: Original SAS<sup>+</sup> Task

*gh*: Specialized Decoupled Search (Gnad & Hoffmann 2018)  
*ts*: Factored Transition Systems (Torralba & Sievers 2019)



# Experiments – Planning Performance

Satisficing IPC Benchmark: 2106 tasks

Domain	GBFS( $h^{FF}$ , PO)				LAMA	
	<i>dec</i>	<i>sas</i>	<i>gh</i>	<i>ts</i>	<i>dec</i>	<i>sas</i>
airport	12	<b>14</b>	11	13	12	11
data-net	9	10	5	11	10	<b>13</b>
floortile11	14	8	17	8	<b>19</b>	7
nomystery	16	9	<b>19</b>	10	18	12
tetris	9	<b>14</b>	11	2	5	<b>14</b>
transport14	<b>20</b>	9	<b>20</b>	<b>20</b>	<b>20</b>	17
...		...			...	
<b>Sum</b> 1059	944	912	<b>980</b>	915	<b>962</b>	942

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## Miura & Fukunaga Factoring (*mf*):

- Effective on **311 of 2106** tasks  
     $\rightsquigarrow$  **Single conclusive leaf**
- **Same coverage** as *sas*
- Max **speed-up** factor: 242

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# Conclusions

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## Summary

- Novel task transformations mimicking decoupled search
- Encoding **leaf dynamics** of decoupled search as **axioms**
- Transformed task's state space  $\overset{\textit{isomorphic}}{\sim}$  Decoupled state space
- Planners can now be **automatically decoupled** leading to **competitive performance**

Full Paper



# Conclusions

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## Future Work

- Reduction of **transformed task size**: e.g., irrelevance pruning
- Preserve costs: **optimal planning**
- Other **reduction techniques as task transformations**: symmetry breaking, partial-order

# References I

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- Gnad, Daniel and Jörg Hoffmann (2018). “Star-Topology Decoupled State Space Search”. In: *AIJ* 257, pp. 24–60.
- Torralba, Álvaro and Silvan Sievers (2019). “Merge-and-Shrink Task Reformulation for Classical Planning”. In: *Proc. IJCAI 2019*, pp. 5644–5652.