

Merging Cartesian Abstractions for Classical Planning

Mauricio Salerno¹, Raquel Fuentetaja¹, David Speck², Jendrik Seipp³
Universidad Carlos III de Madrid¹, Basel University², Linköping University³

Cartesian Abstractions in Planning

- **Optimal Classical Planning:** cheapest sequence of actions that achieve the goals
- **A*:** prominent solution method, needs *domain independent* heuristics
- **Abstractions:** solve a simpler version of the problem, use *solution* cost as heuristic
- **Cartesian Abstractions:** prominent abstraction type, built with **CEGAR**

Task Decomposition

- One big abstraction: converges to h^* , suffers from **diminishing returns**
- One task per goal, and builds small abstractions
- **Cost partitioning** combines the estimates of the small abstractions **admissibly**

Limitations of each approach:

- **Big abstraction:** considers all goal interactions, expensive to build
- **Small abstractions:** cheap to build, misses goal interactions

New approach: Multi-Goal Cartesian Abstractions

How to select which subsets of goals to build abstractions for?

- Too many alternatives: $2^n - 1$ subsets for n goals
- Can't know in advance what is useful

Systematic approach:

- Start with **single-goal** abstractions
- Build **multi-goal** (first pairs, then triples, etc.) abstractions if resources allow it

Merging Abstractions

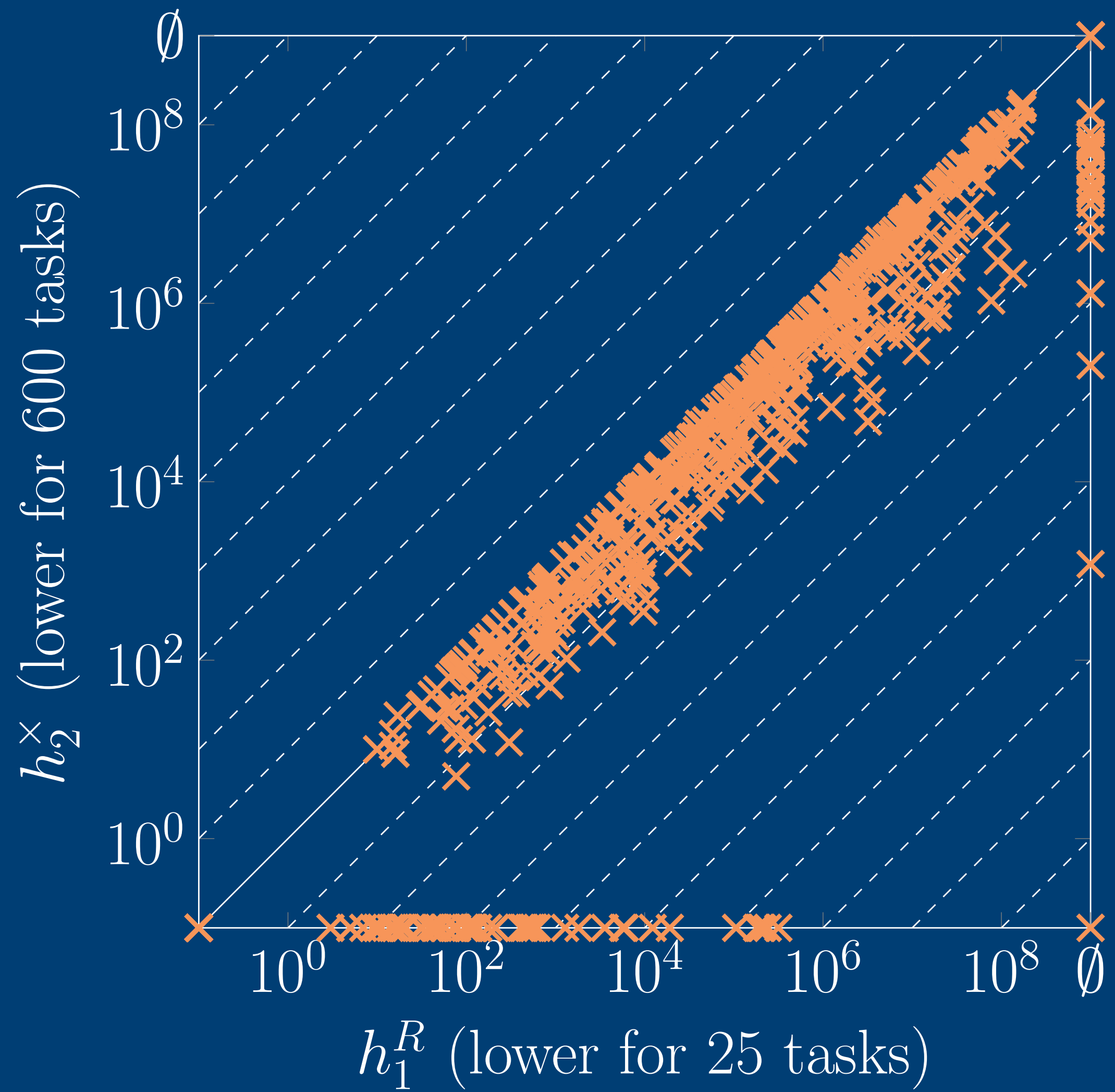
Avoid repeating work by **merging** existing abstractions:

- For **2-goal** abstraction with goals i, j : **merge 1-goal** abstractions for i and j
- **Merging:** synchronized product of transition systems
- **Efficiency:** avoid re-creating abstractions from scratch

Future Work

- Identify promising goal subsets to build multi-goal abstractions
- Cost partitioning methods tailored for multi-goal abstractions

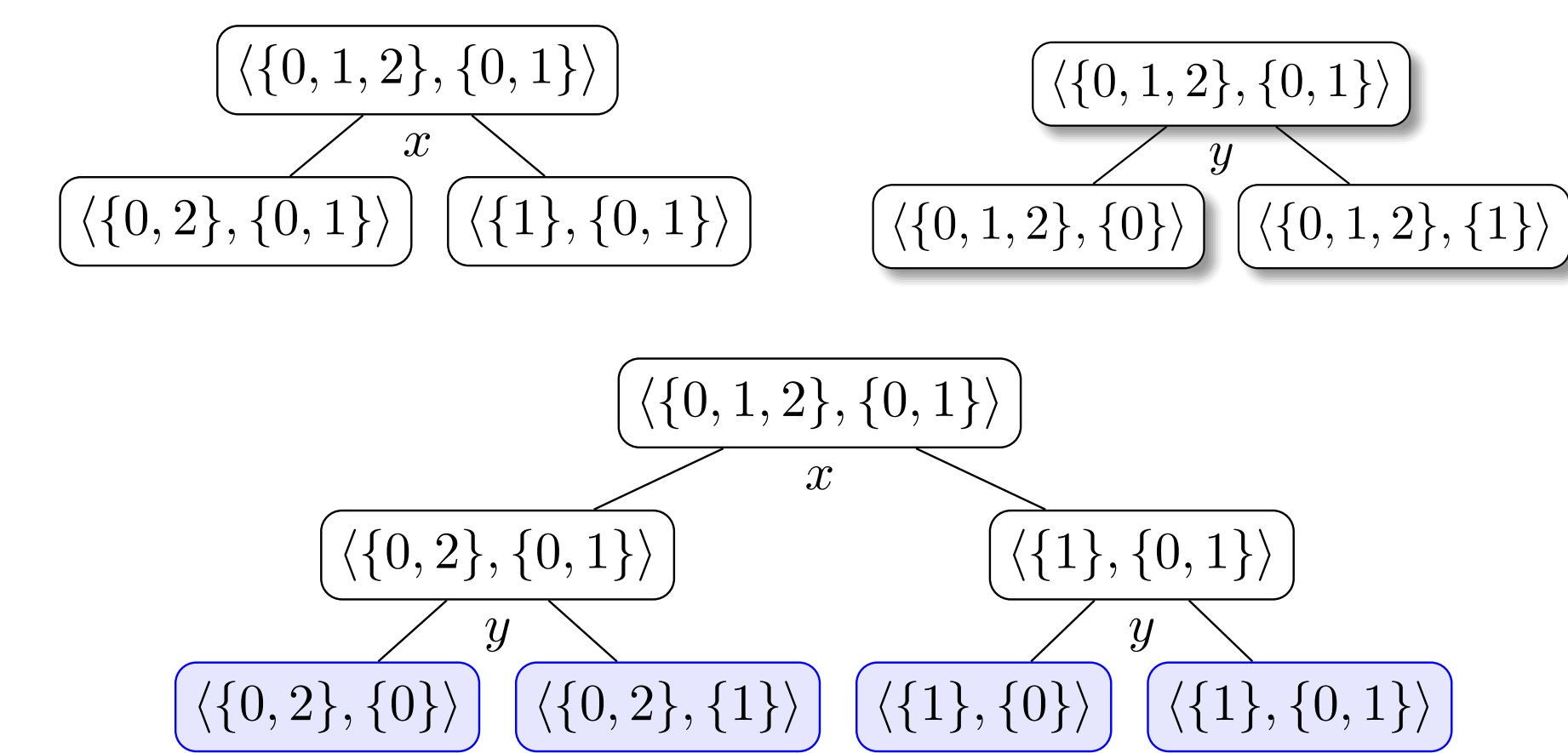
Finding the sweet spot between one big abstraction and many small ones



Check out the paper!

Merge Cartesian Abstractions?

- $v = \{x, y\}$
- $\mathcal{I} = \{x = 0, y = 0\}$
- $\mathcal{G} = \{x = 1, y = 1\}$
- $dom(x) = \{0, 1, 2\}$
- $dom(y) = \{0, 1\}$



What About Cost Partitioning?

More abstractions can produce **worse heuristics!**

When is it *always* better to have more abstractions?

What if superseded abstractions are **dropped**?

Cost Partitioning	Keep	Drop
Optimal	✓	✓
Saturated Post-hoc	✓	✗
Saturated	✗	✗

More Results!

		Refine					Merge & Refine				+Landmarks	
		h^G	h_1^R	h_2^R	h_3^R	h_4^R	h_2^x	h_3^x	h_4^x	h_∞^x	h_1^L	h_2^L
Refine	h^G	-	11	7	7	6	6	5	5	5	10	6
	h_1^R	14	-	0	1	0	0	0	0	0	1	3
	h_2^R	20	12	-	1	2	2	3	3	3	9	7
	h_3^R	22	14	5	-	3	6	6	6	6	10	10
	h_4^R	21	12	6	3	-	4	3	3	3	8	9
M & R	h_2^x	25	19	14	12	11	-	3	3	3	11	6
	h_3^x	25	20	14	13	12	4	-	1	2	12	8
	h_4^x	25	20	14	13	12	3	0	-	1	12	8
	h_∞^x	24	19	13	12	11	2	0	0	-	11	7
+L	h_1^L	22	13	11	11	11	9	8	8	8	-	2
	h_2^L	24	19	16	14	15	9	11	11	11	11	-
C		844	853	868	875	875	888	889	888	887	1009	1026